

5M/PHY-302 Syllabus-2023

2 0 2 5

(Nov-Dec)

FYUP : 5th Semester Examination

MAJOR

PHYSICS

(Thermal and Statistical Physics)

PHY-302

Marks : 75

Time : 3 hours

*The figures in the margin indicate full marks
for the questions*

Answer any **ten** questions

1. Derive the general expression for Maxwell's thermodynamical relations and hence derive the four Maxwell's thermodynamic relations.

$5\frac{1}{2}+2=7\frac{1}{2}$

2. What is Joule-Thomson cooling? Deduce the thermodynamic expression for the Joule-Thomson coefficient, μ . Prove that for a perfect gas, $\mu = 0$.

$1+4\frac{1}{2}+2=7\frac{1}{2}$

3. (a) Prove the following thermodynamic relation : 2½

$$C_P - C_V = T \left(\frac{\partial P}{\partial T} \right)_V \left(\frac{\partial V}{\partial T} \right)_P$$

- (b) Derive the first and second Tds equations. 2½+2½=5
4. (a) Deduce Clapeyron's latent heat equation using Maxwell's thermodynamic relations. Discuss briefly the effect of change in pressure on boiling point. 3½+1=4½

- (b) Calculate under what pressure ice freezes at 272 K if the change in specific volume, when 1 kg of water freezes, is $91 \times 10^{-6} \text{ m}^3$. Given, latent heat of ice = $3.36 \times 10^5 \text{ J}\cdot\text{kg}^{-1}$. 3

5. (a) What is Gaussian distribution? Obtain the expression for it. 1+5=6

- (b) Find the probability density function for the normal distribution where mean = 4, standard deviation = 2 and random variable, $x = 3$. 1½

6. (a) Derive Stirling's approximation $\ln(n!) = n \ln n - n$ 3½

- (b) A bag contains 7 red, 8 yellow and 5 green balls. The balls are drawn at random from the bag. What is the probability of selecting (i) red ball and (ii) yellow ball? 2+2=4

7. (a) Explain the terms 'phase space' and 'momentum space'. 1+1=2

- (b) Calculate the number of phase cells, and hence energy, in the energy range 0 to E for a linear harmonic oscillator of mass m and frequency ν . 5½

8. Establish Liouville's theorem and explain its physical significance. 6+1½=7½

9. Define entropy. Deduce Boltzmann's entropy probability relation $S = k_B \ln W$, where symbols carry their usual meaning. 1½+6=7½

10. What is canonical ensemble? Obtain the expression for the probability distribution function in a canonical ensemble. 1½+6=7½

11. State and prove the law of equipartition of energy. 1½+6=7½

12. (a) What is partition function? Mention its importance and write down its relation with entropy of a thermodynamic system. 1½+1½+1½=4½

(b) At what temperature will the average speed of molecules of hydrogen gas be doubled the average speed of molecules of oxygen at 300 K? 3

13. (a) Using Maxwell-Boltzmann distribution function, find the total internal energy and specific heat at constant volume of a perfect gas. 4½

(b) For O₂ gas at NTP, calculate (i) most probable speed and (ii) root mean square speed.

Given, Boltzmann's constant, $k_B = 1.38 \times 10^{-23} \text{ JK}^{-1}$ and Avogadro's number, $N_A = 6.02 \times 10^{23} / \text{mole}$. $1\frac{1}{2} + 1\frac{1}{2} = 3$

14. What are the basic postulates of Fermi-Dirac statistics? Derive an expression for probability distribution of particles governed by Fermi-Dirac statistics. $1\frac{1}{2} + 6 = 7\frac{1}{2}$

15. Write down the expression for Bose-Einstein distribution function. Apply Bose-Einstein statistics to deduce Planck's radiation law in terms of wavelength. $1 + 6\frac{1}{2} = 7\frac{1}{2}$

★ ★ ★